

First Problem Set Assignment: Backus-Naur Form (BNF)

Abstract

The first problem set is intended to demonstrate Backus-Naur Form and its use in demonstrating the syntax of a programming language. Defining the grammar of a language demonstrates the ways in which a language is structured, any 'legal' combination of expressions that can be constructed in the confines of the language. Designing a parse tree allows for a visual representation of the syntax of the language, tracing the process from node to node to construct an expression in the language. Tasks 2 through 11 allowed for practice in constructing grammars and parse trees for predefined languages.

Task 1: BNF?

Backus-Naur Form is a way to logically reason the syntax of a programming language. It is a way to demonstrate how a language is interpreted by showing the permitted structures and expressions that are valid for that specific language. BNF is significant to programming because it demonstrates the structure and syntax of a language, shaping the functionality and limitations of a programming language.

Task 2

$\langle \text{string} \rangle ::= \langle +\text{string} \rangle | \langle -\text{string} \rangle | \langle \text{empty} \rangle$
 $\langle +\text{string} \rangle ::= + \langle +\text{string} \rangle | \langle +\text{string} \rangle | \langle \text{empty} \rangle$
 $\langle -\text{string} \rangle ::= - \langle -\text{string} \rangle | \langle -\text{string} \rangle | \langle \text{empty} \rangle$
 $\langle \text{empty} \rangle ::= () \langle \text{string} \rangle | ()$

Task 3

1. $()$

$\langle \text{string} \rangle :$
|
 $\langle \text{empty} \rangle$
|
 $()$

2. $(-)(++)$

$\langle \text{string} \rangle$
|
 $\langle -\text{string} \rangle$
/ \
 $(- \langle -\text{string} \rangle$
| \
 $-) \langle \text{string} \rangle$
|
 $\langle +\text{string} \rangle$
/ \
 $(+ \langle +\text{string} \rangle$
| \
 $+ \langle +\text{string} \rangle$
| \
 $+ \langle \text{empty} \rangle$

Task 4

$\langle \text{string} \rangle ::= \langle 1 \rangle | \langle 2 \rangle | \langle 3 \rangle | \langle 0 \rangle$
 $\langle 1 \rangle ::= | \langle \text{string} \rangle | | \langle \text{empty} \rangle$
 $\langle 2 \rangle ::= 2 \langle \text{string} \rangle | 2 \langle \text{empty} \rangle$
 $\langle 3 \rangle ::= 3 \langle \text{string} \rangle | 3 \langle \text{empty} \rangle$
 $\langle 0 \rangle ::= 0 \langle \text{string} \rangle | 0 \langle \text{empty} \rangle$
 $\langle \text{empty} \rangle ::= ' '$

Task 5

0

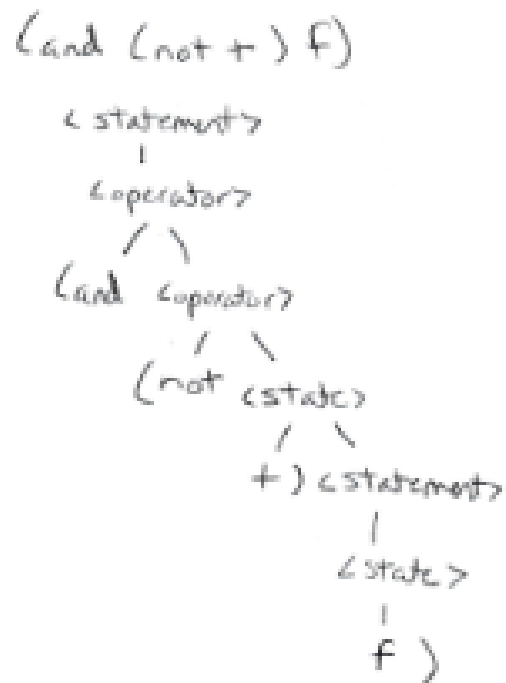
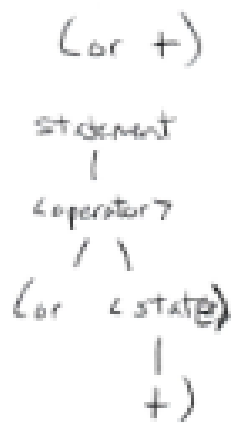
$\langle \text{string} \rangle$
 $|$
 $\langle 0 \rangle$
 $| \backslash$
 $0 \langle \text{empty} \rangle$
 $| \backslash$

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$\langle \text{string} \rangle$
 $|$
 $\langle 3 \rangle$
 $/ \backslash$
 $3 \langle \text{string} \rangle$
 $|$
 $\langle 2 \rangle$
 $/ \backslash$
 $2 \langle \text{string} \rangle$
 $|$
 $\langle 1 \rangle$
 $/ \backslash$
 $1 \langle \text{string} \rangle$
 $|$
 $\langle 0 \rangle$
 $/ \backslash$
 $0 \langle \text{string} \rangle$
 $|$
 $\langle 0 \rangle$
 $/ \backslash$
 $0 \langle \text{empty} \rangle$
 $| \backslash$

Task 6 $\langle \text{statement} \rangle ::= \langle \text{operator} \rangle \mid \langle \text{state} \rangle$
 $\langle \text{operator} \rangle ::= (\text{and } \langle \text{state} \rangle) \mid (\text{or } \langle \text{state} \rangle) \mid (\text{not } \langle \text{state} \rangle) \mid$
 $(\text{and } \langle \text{operator} \rangle) \mid (\text{or } \langle \text{operator} \rangle) \mid (\text{not } \langle \text{operator} \rangle)$
 $\langle \text{state} \rangle ::= + \mid f \mid \langle \text{statement} \rangle \mid f \langle \text{statement} \rangle$

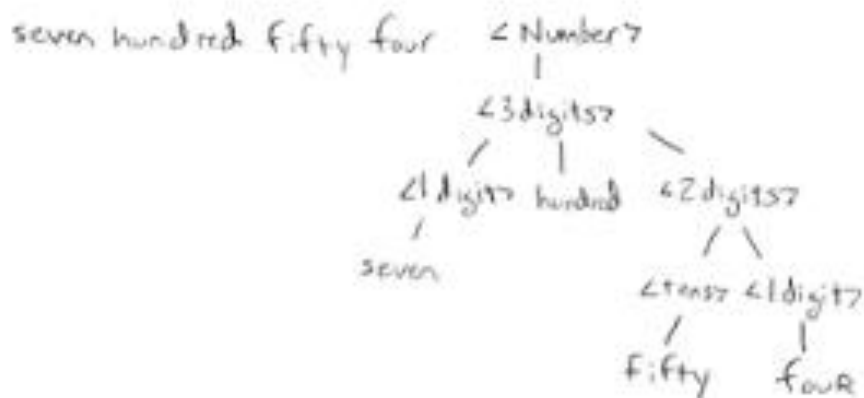
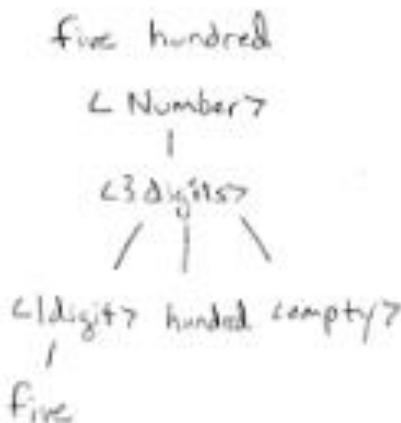
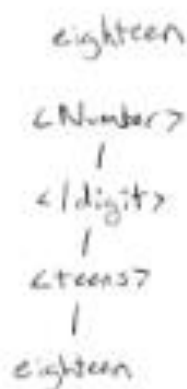
Task 7



Task 8

$\langle \text{Number} \rangle ::= \langle 3 \text{ digits} \rangle \mid \langle 2 \text{ digits} \rangle \mid \langle 1 \text{ digit} \rangle$
 $\langle 1 \text{ digit} \rangle ::= \text{one} \mid \text{two} \mid \text{three} \mid \text{four} \mid \text{five} \mid \text{six} \mid \text{seven} \mid \text{eight} \mid \text{nine} \mid \text{ten}$
 $\langle \text{tens} \rangle ::= \text{eleven} \mid \text{twelve} \mid \text{thirteen} \mid \text{fourteen} \mid \text{fifteen} \mid \text{sixteen} \mid \text{seventeen} \mid \text{eighteen} \mid \text{nineteen} \mid \text{ten}$
 $\langle 2 \text{ digits} \rangle ::= \langle \text{tens} \rangle \langle 1 \text{ digit} \rangle \mid \langle \text{tens} \rangle$
 $\langle \text{tens} \rangle ::= \text{twenty} \mid \text{thirty} \mid \text{forty} \mid \text{fifty} \mid \text{sixty} \mid \text{seventy} \mid \text{eighty} \mid \text{ninety}$
 $\langle 3 \text{ digits} \rangle ::= \langle 1 \text{ digit} \rangle \text{hundred} \langle 2 \text{ digits} \rangle \mid \langle 1 \text{ digit} \rangle \text{hundred} \langle \text{empty} \rangle$

Task 9



Task 10

$\langle \text{Colorfun} \rangle ::= \langle \text{describe} \rangle \mid \langle \text{add} \rangle \mid \langle \text{show} \rangle \langle \text{colors} \rangle$

$\langle \text{describe} \rangle ::= \langle \text{colors} \rangle \mid \langle \text{C\#} \rangle$

$\langle \text{C\#} \rangle ::= \langle \text{C1} \rangle \mid \langle \text{C2} \rangle \mid \langle \text{C3} \rangle \mid \langle \text{C4} \rangle \mid \langle \text{C2B} \rangle$

$\langle \text{show} \rangle ::= \langle \text{colors} \rangle \mid \langle \text{C\#} \rangle$

$\langle \text{add} \rangle ::= \langle \text{N} \rangle \langle \text{N} \rangle \langle \text{N} \rangle \langle \text{color} \rangle \mid \langle \text{N} \rangle \langle \text{N} \rangle \langle \text{N} \rangle \langle \text{N} \rangle \langle \text{color} \rangle \mid$

$\langle \text{color} \rangle \langle \text{C\#} \rangle \mid \langle \text{N} \rangle \langle \text{N} \rangle \langle \text{N} \rangle \langle \text{C\#} \rangle$

$\langle \text{N} \rangle ::= 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9 \mid 10 \mid 11 \mid 12 \mid 13 \mid 14 \mid \dots \mid 255$

$\langle \text{Colors} \rangle ::= \text{light red} \mid \text{red} \mid \text{purple}$

Task 11

